

Stability of Target Resonance Modes: Ina Quadrature Polarization Context

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ABSTRACT

The paper present a studyon the noise effect whenextracting the resonance residue in a quadrature polarization setup. The accuracy and stability of the mode quadrature residues is necessary to construct the polarization matrix, and subsequently, derive a robust polarization states of the receiver antenna. However, with lower signal-to-noise ratios the extraction performance will degrade; in this regards, the in-phase and quadrature components of the baseband signal demonstrated improvedextraction performancewhen used. Here, a case of two disjoint wires is used to verify this approach.

Keywords-Resonance Theory, Method of Pencil, Singularity Expansion, Radar target, Polarization.

I. INTRODUCTION

According to the model-based signature, namely Singularity Expansion Method (SEM) model, the late time of the target impulse response can be expressed as a sum of resonance modes with terms, namelyresonant frequency and residue, relating to the dimensions and composition of the target. Alongsideresonance based signatures when identifying radar targets, researchers have incorporatedpolarization descriptions, i.e. vector or matrix, to form enhanced feature set [1-4]. Particularly of interest is the characteristic polarizationstateswhich represent the power critical conditions at the antenna's terminal. Once based on the target resonance modes, the polarization set can reveal the target shape attributes like elongation, symmetry and tilt degrees [5, 6].

To fully obtain the target resonance modes (related in turn to itsindividual substructures), radar illumination usesa widebandcarrier-free (Baseband) radio wave. Then either extracted temporally, for example, by Method Pencil-of-Function (MPOF)[7]or estimated spectrally from peaks in magnitude spectrum for high-Q targets[8]. The resonance modescan be incorporate in a setup of quadrature polarization channels to derivetheir respective polarizationset. However, to attain robust extraction, the quadrature polarized residue terms, i.e. residues matrix, of a mode should be stably extractable; else a residue term will be missed or misaligned in the polarization matrix and thus leading to ill estimatedpolarization set.

Therefore, proper extraction is necessary so not to omit or misalign a resonance along any polarization direction in this matrix. Unfortunately, omitting or misaligning a resonance can occur if the residue-to-noise ratio (*SNR*) is low. To overcome the low *SNR*drawback, the oscillatory behaviors of the resonance should be enhanced by extending the late time portion. Therefore, theauthor proposes to implement the extraction using real (in-phase) and imaginary (quadrature) versionsof the baseband signal. The real and imaginary parts have extended late time because of their more prominent oscillatory behavior compared to the original baseband signal.

This paper is outlined as follows: Section II presents a formulation to derive the polarization angles. Section III present the results which include descriptionof the simulation procedures and the extraction performance of the proposed technique. Section IVreaches conclusions and indicates directions for further work.

II. FORMULATION

In phasor form, the complex frequency spectrum $F(\omega)$ is expressed in term of the signal magnitude $|A|$ response and phase ϕ response, at angular frequency ω , as follows

$$Y(\omega) = |A(\omega)| \cdot \exp(\phi(\omega)) \quad (1)$$

Or in complex form as

$$Y(\omega) = \text{Re}[F(\omega)] + j \cdot \text{Im}[F(\omega)] \quad (2)$$

Where

$$\begin{aligned} \text{Re}[F(\omega)] &= |A(\omega)| \cdot \cos(\phi(\omega)) \text{ , i.e. in-phase} \\ \text{Im}[F(\omega)] &= |A(\omega)| \cdot \sin(\phi(\omega)) \text{ , i.e. quadrature} \end{aligned}$$

If the $\text{Re}[F(\omega)]$ or $\text{Im}[F(\omega)]$ is substituted instead of the absolute magnitude $|A|$ in (1), then the

new magnitude spectrum will have the shape of $|A(\omega)\cos(\varphi)|$ or $|A(\omega)\sin(\varphi)|$ spectrums.

Then by applying a Fourier Transformer operator $F^{-1}(\cdot)$ to $Y()$, $Y_{re}()$ and $Y_{im}()$, the temporal baseband responses $y(t)$, $y_{re}(t)$ and $y_{im}(t)$ are obtained. For a quadrature polarization directions in orthogonal linear basis, e.g. (h,v) , the temporal baseband responses in a quadrature set $\mathbf{y}(t_o)$, forms a $R^{2 \times 2}$ matrix, and according to SEM model will be expressed as follows

$$\mathbf{y}(t_o) = \sum_{n=1}^M \mathbf{C}_n \cdot e^{-(\sigma_n + j\omega_n)t_o} \quad (3)$$

Such that

$$\mathbf{C}_n = \begin{bmatrix} c_n^{hh} & c_n^{hv} \\ c_n^{vh} & c_n^{vv} \end{bmatrix} \quad (4)$$

Here $t_o > T_L$, and T_L denotes the late time onset after which the incident wave has totally passed the target. The mode terms σ , ω and c denote the: damping factor, resonant frequency and complex residue. The modal order M gives the number of modes presumably excited. The subscripts denote the transmitter and receiver polarization directions, where hh and vv denote the co-polarized scattering directions or channels, while vh and hv denote the cross-polarized scattering channels (reciprocal for monostatic case).

III. SIMULATION & RESULTS

For this purpose, a set of two disjoint and parallel wires is used to validate this. The longer one is 100 units of length and rotated 10° from a reference axis, whereas the shorter one is 50 units of length, separated from the longer wire by 20 units of length and rotated 40° . In general, the plane wave direction is set normal to the wires, where the simulated backscattered data were generated in frequency-domain by method of moments algorithm (MoM) using FEKO [9].

3.1 Temporal and spectral domains

Firstly, signals are corrupted by additive white gaussian noise assuming the signal power in each channel is 0dBW, i.e. this is not a case of background noise. Secondly, the signals are filtered by a Gaussian window to create the effect of a Gaussian shaped impulse, and then the frequency spectrum is transformed to the time-domain by Fourier Transform operator $F^{-1}(\cdot)$. As depicted in Fig.1 and Fig.2 for two cases of high and low SNR, the signals y and y_{re} with respective Y and Y_{re} as insets are shown. Comparing both signals in time domain, it is noted that y_{re} demonstrates better oscillatory behaviour as the late time portion extends beyond 150 units time with lesser damping

effect. While in the frequency domain, Y_{re} has more localized spectrum, i.e. high Q-peaks.

3.2 Residue extraction vs. noise: accuracy and stability

Initially, the residue terms of the resonance modes are extracted by applying the MPOF to the FFT time signal $F^{-1}(\cdot)$ as depicted in Fig.3 and Fig.4 for the three set of signals. In Fig.3 with $SNR=60dB$, the residues terms of the quadrature channels are well aligned at each resonant frequency. In comparison, the y_{re} and y_{im} signals have stronger residues, i.e. more stability, as they are more extended in time, moreover, the residues strength and location patterns are similar for all signal as residues in the HH are the strongest while in VV are the weakest, subsequently, reflecting the polarization state of the mode. In Fig.4 with $SNR=0dB$, the residues strength pattern is less affected compared by the effect on their location pattern.

Table I, Table II and Table III present the accuracy results of extraction for the temporal baseband responses $y(t)$, $y_{re}(t)$ and $y_{im}(t)$ with SNR level from -5dB to 30dB. The accuracy is quantified by how much (in a percentage) the reconstructed signal (from the estimated modes) resemble the original signal. The results show that the modes terms in y_{re} and y_{im} signals are overall more accurate compared to the baseband signal.

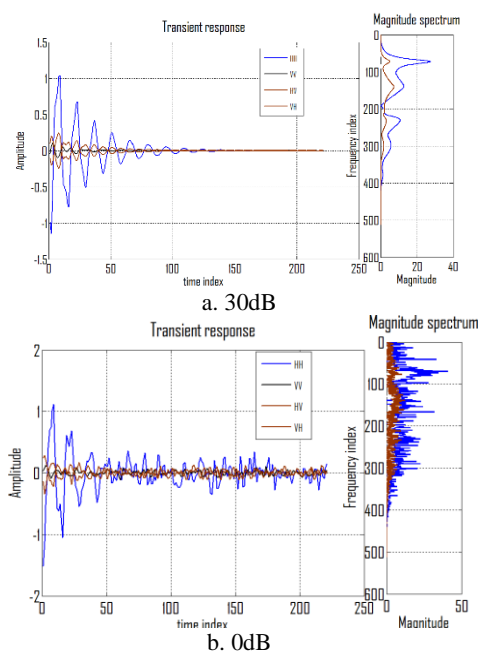


Fig.1. The temporal and spectral responses of signal $y(t)$ vs. SNR level.

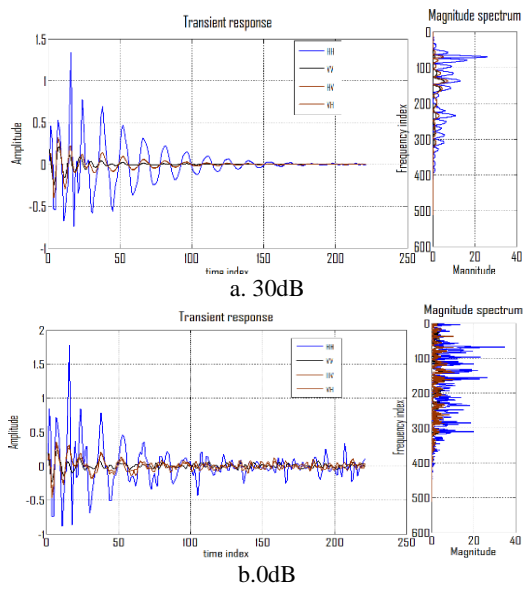


Fig.2.The temporal and spectral responses of signal $y_{re}(t)$ vs.SNRlevel.

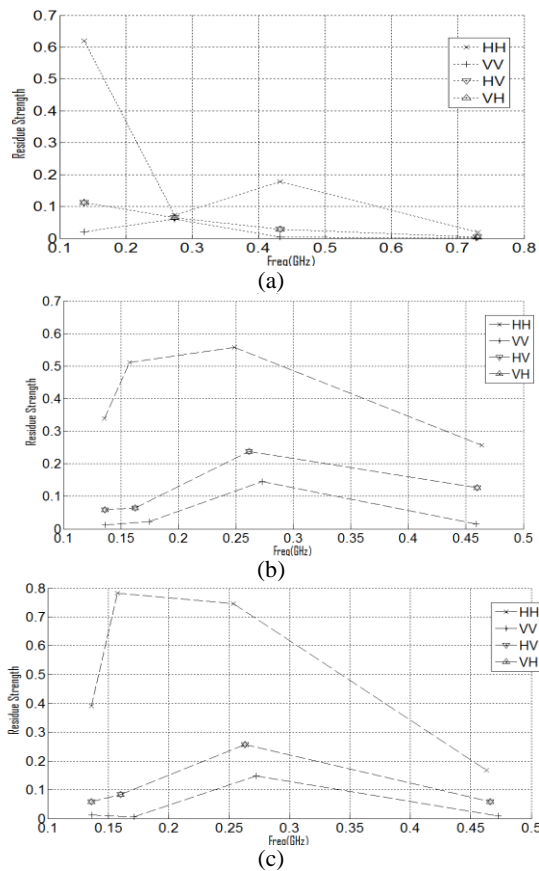


Fig.3.The residue distribution with 60dB SNRfor (a) $f^1(Y(f))$, (b) $f^1(Re[Y(f)])$ and (c) $f^1(Im[Y(f)])$.

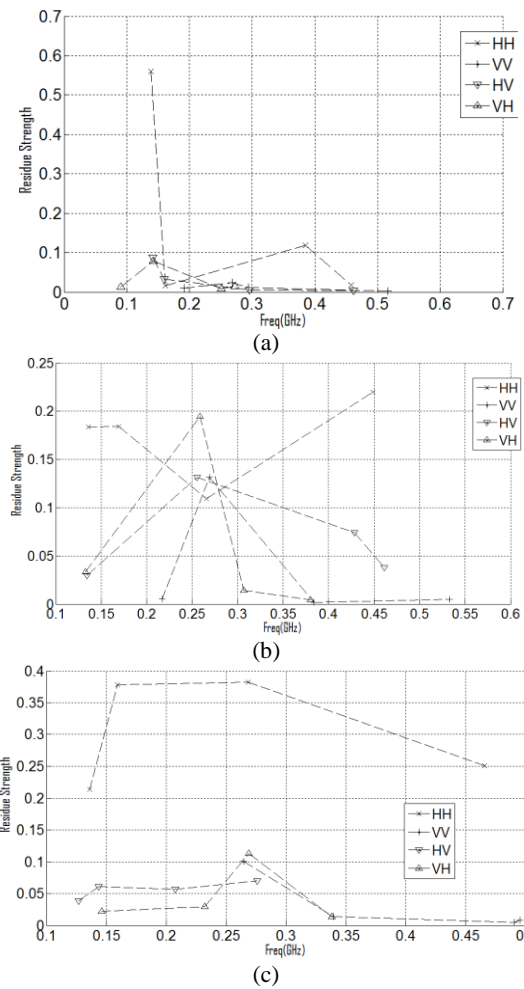


Fig.4.The residue distribution with 0dB SNRfor (a) $f^1(Y(f))$, (b) $f^1(Re[Y(f)])$ and (c) $f^1(Im[Y(f)])$

TABLE I.THE ACCURACY OF THE SEM MODEL TERMS FORCOHERENT SPECTRUM Y(F)

| dB | HH | VV | HV | VH | Mean per SNR |
|------------------|------|------|------|------|-----------------------|
| 30 | 99.8 | 97.6 | 99.5 | 99.4 | 99.1 |
| 25 | 99.4 | 94.2 | 98.1 | 98.3 | 97.5 |
| 20 | 97.4 | 82.2 | 94.2 | 94.1 | 92.0 |
| 15 | 94.2 | 56.5 | 81.5 | 83.1 | 78.8 |
| 10 | 87.6 | 26.9 | 53.0 | 60.9 | 57.1 |
| 5 | 63.7 | 12.8 | 37.0 | 46.5 | 40.0 |
| 0 | 49.4 | 15.5 | 10.1 | 27.6 | 25.6 |
| -5 | 31.8 | 14.5 | 16.7 | 16.7 | 19.9 |
| Mean per channel | 77.9 | 50.0 | 61.3 | 65.8 | 63.8 overall accuracy |

TABLE II. THE ACCURACY OF THE SEM MODEL TERMS FORRE [(Y(F))

| dB | HH | VV | HV | VH | Mean per SNR |
|------------------|------|------|------|------|-----------------------|
| 30 | 80.3 | 99.3 | 93.9 | 94.1 | 91.9 |
| 25 | 79.9 | 98.4 | 94.0 | 93.8 | 78.2 |
| 20 | 79.1 | 97.5 | 92.5 | 92.5 | 76.3 |
| 15 | 75.7 | 94.4 | 91.1 | 91.2 | 73.5 |
| 10 | 74.2 | 80.7 | 79.4 | 77.9 | 64.4 |
| 5 | 59.1 | 62.9 | 46.2 | 55.9 | 45.8 |
| 0 | 38.3 | 40.4 | 42.7 | 20.0 | 28.3 |
| -5 | 31.2 | 11.1 | 25.8 | 27.5 | 18.1 |
| Mean per channel | 64.7 | 73.1 | 70.7 | 69.1 | 69.4 overall accuracy |

TABLE III. THE ACCURACY OF THE SEM MODEL TERMS FORIM [(Y(F))

| dB | HH | VV | HV | VH | Mean per SNR |
|------------------|------|------|------|------|-----------------------|
| 30 | 82.5 | 99.4 | 94.3 | 94.6 | 92.7 |
| 25 | 82.0 | 98.8 | 94.3 | 94.4 | 92.4 |
| 20 | 81.5 | 97.8 | 92.6 | 93.1 | 91.2 |
| 15 | 78.6 | 93.7 | 90.2 | 91.0 | 88.4 |
| 10 | 74.2 | 89.0 | 80.3 | 76.3 | 79.9 |
| 5 | 57.8 | 69.6 | 67.1 | 54.7 | 62.3 |
| 0 | 47.9 | 36.1 | 31.9 | 43.6 | 39.9 |
| -5 | 21.3 | 16.9 | 21.1 | 26.5 | 21.4 |
| Mean per channel | 65.7 | 75.2 | 71.5 | 71.8 | 71.0 overall accuracy |

IV. CONCLUSIONS

The in-phase or quadrature filtered signal of a wideband baseband signal has better oscillatory behaviors which makes them relatively more immune to noise when extracting the resonance modes. This is an essential requirement when mode residues are used to construct the polarization matrix, as missing or misaligning a residue in the matrix will lead to inaccurate polarization states. The residue strength pattern is less affected by noise relatively to their location pattern. Finally, investigating the performance of the characteristic polarization states based on the in-phase or quadrature components of the signal can be a subject of further studies.

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